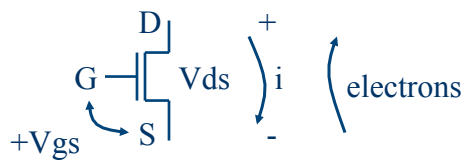
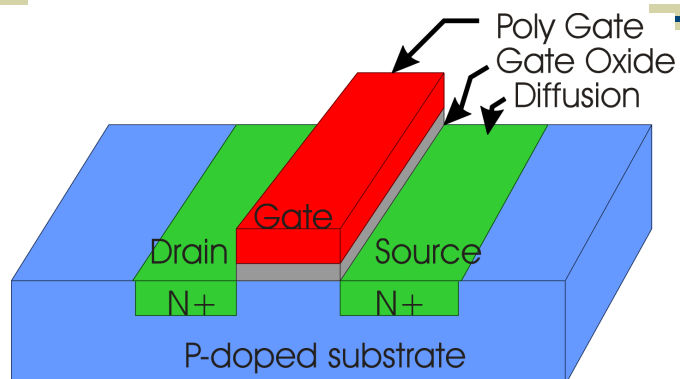


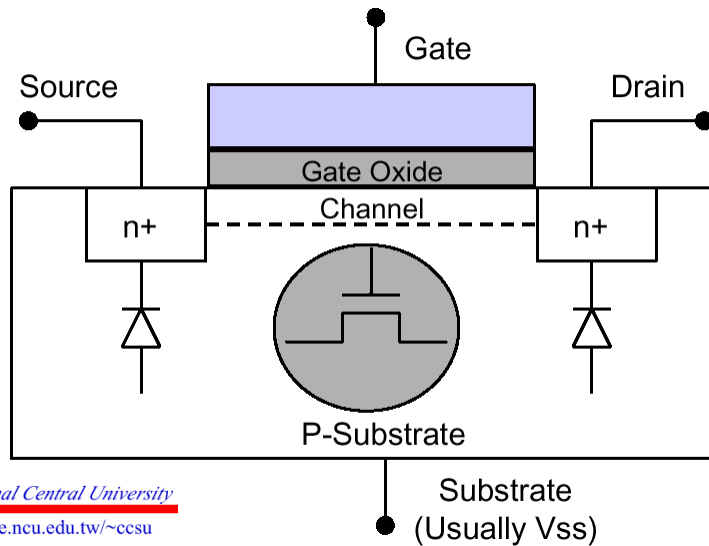
CS/ECE 5710/6710

MOS Transistor Models Electrical Effects Propagation Delay

N-type Transistor

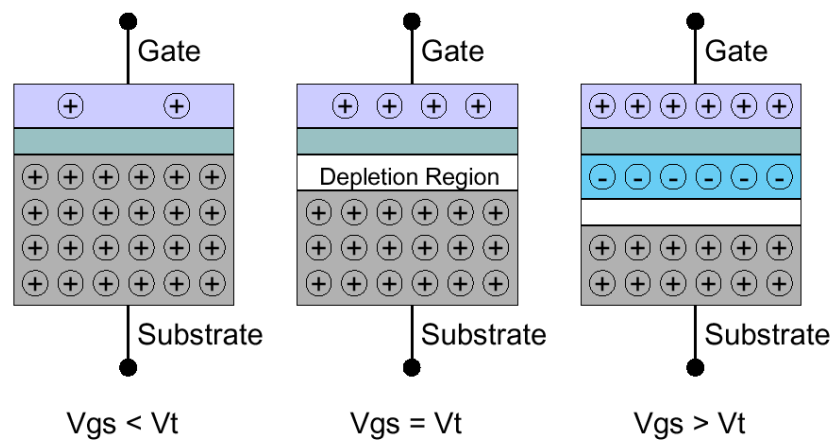


Another Cutaway View



National Central University
www.ee.ncu.edu.tw/~ccsu

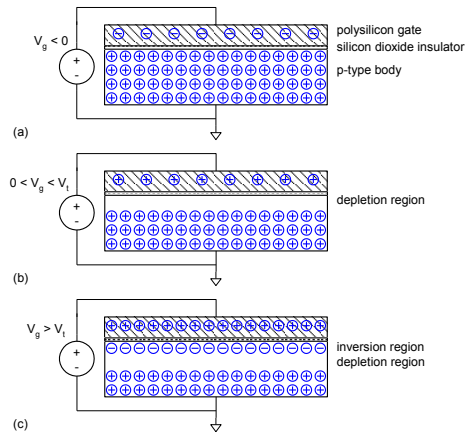
V_{gs} Forms a Channel



V_t : The threshold voltage to turn on the transistor

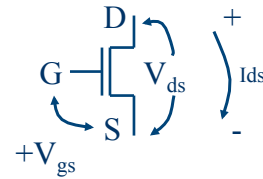
MOS Capacitor

- ◆ Gate and body form MOS capacitor
- ◆ Operating modes
 - Accumulation
 - Depletion
 - Inversion



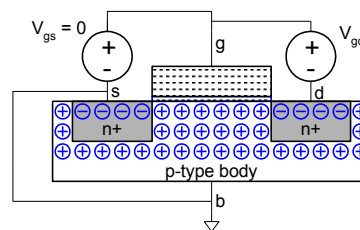
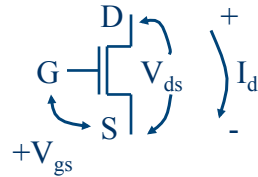
Transistor Characteristics

- ◆ Three conduction characteristics
 - Cutoff Region
 - No inversion layer in channel
 - $I_{ds} = 0$
 - Nonsaturated, or linear region
 - Weak inversion of the channel
 - I_{ds} depends on V_{gs} and V_{ds}
 - Saturated region
 - Strong inversion of channel
 - I_{ds} is independent of V_{ds}
 - As an aside, at very high drain voltages:
 - “avalanche breakdown” or “punch through”
 - Gate has no control of I_{ds} ...



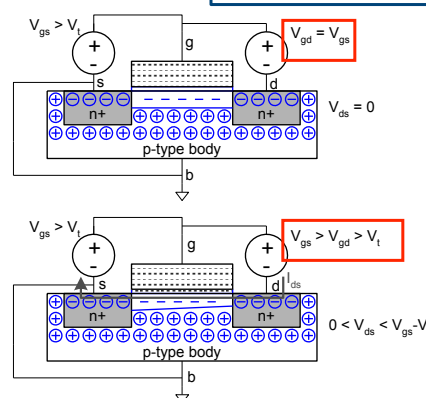
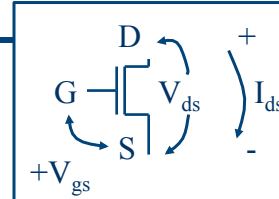
nMOS Cutoff: $V_{gs} < V_t$

- ♦ No channel
- ♦ $I_{ds} = 0$



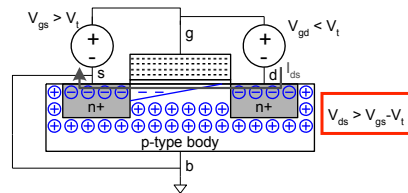
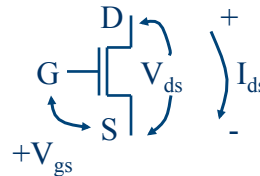
nMOS Linear: $V_{gs} > V_t$, small V_{ds}

- ♦ Channel forms
- ♦ Current flows from d to s
 - e^- from s to d
- ♦ I_{ds} increases with V_{ds}
- ♦ Similar to linear resistor



nMOS Saturation: $V_{ds} > V_{gs} - V_t$

- ◆ Channel pinches off
 - Conduction by drift because of positive drain voltage
 - Electrons are injected into depletion region
- ◆ I_{ds} independent of V_{ds}
- ◆ We say that the current saturates
- ◆ Similar to current source

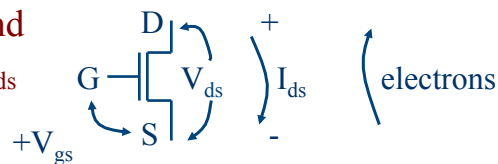


Basic N-Type MOS Transistor

- ◆ Conditions for the regions of operation

- **Cutoff:** If $V_{gs} < V_t$ then I_{ds} is essentially 0
 - V_t is the “Threshold Voltage”
- **Linear:** If $V_{gs} > V_t$ and $V_{ds} < (V_{gs} - V_t)$ then I_{ds} depends on both V_{gs} and V_{ds}
 - Channel becomes deeper as V_{gs} goes up

- **Saturated:** If $V_{gs} > V_t$ and $V_{ds} > (V_{gs} - V_t)$ then I_{ds} is essentially constant (Saturated)



Transistor Gain (β)

$$\beta = (\underbrace{\mu \epsilon / t_{\text{ox}}}_{\text{Process-dependent}}) \underbrace{(W/L)}_{\text{Layout dependent}}$$

- μ = mobility of carriers ($\text{cm}^2 / \text{V} \cdot \text{s}$)
 - Note that N-type is $\sim 3X$ as good as P-type
- ϵ = permittivity of gate insulator (oxide)
 - $\epsilon = 3.9 \epsilon_0$ for SiO_2 ($\epsilon_0 = 8.85 \times 10^{-14} \text{ F/cm}$)
- t_{ox} = thickness of gate insulator (oxide)
- Also, $\epsilon/t_{\text{ox}} = C_{\text{ox}}$ The oxide capacitance
 - $\beta = (\mu C_{\text{ox}})(W/L) = k'(W/L) = KP(W/L)$
- ◆ *Increase W/L to increase gain*

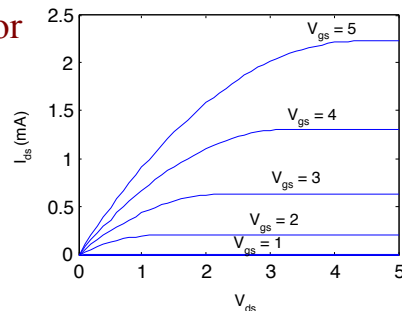
Example

- ◆ We will be using an old $0.5/0.6 \mu\text{m}$ process for your project

- From ON Semiconductor
- $t_{\text{ox}} = 100 \text{ \AA}$
- $\mu = 350 \text{ cm}^2 / \text{V} \cdot \text{s}$
- $V_t = 0.7 \text{ V}$

- ◆ Plot I_{ds} vs. V_{ds}

- $V_{\text{gs}} = 0, 1, 2, 3, 4, 5$
- Use $W/L = 4/2 \lambda$



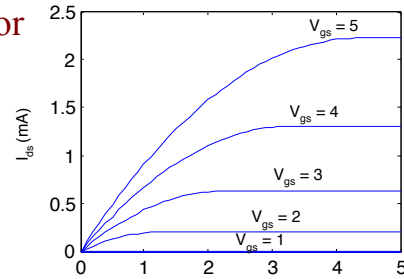
$$\beta = \mu C_{\text{ox}} \frac{W}{L} = (350) \left(\frac{3.9 \cdot 8.85 \cdot 10^{-14}}{100 \cdot 10^{-8}} \right) \left(\frac{W}{L} \right) = 120 \frac{W}{L} \mu\text{A}/\text{V}^2$$

Example

- ◆ We will be using an old 0.5/0.6 μm process for your project

- From ON Semiconductor

- $t_{\text{ox}} = 100 \text{ \AA}$
- $\mu = 350 \text{ cm}^2/\text{V}\cdot\text{s}$
- $V_t = 0.7 \text{ V}$
- $C_{\text{ox}} = \epsilon/t_{\text{ox}}$



$$\beta = \mu C_{\text{ox}} \frac{W}{L} = (350) \left(\frac{3.9 \cdot 8.85 \cdot 10^{-14}}{100 \cdot 10^{-8}} \right) \left(\frac{W}{L} \right) = 120 \frac{W}{L} \mu\text{A}/\text{V}^2$$

“Saturated” Transistor

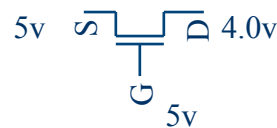
- ◆ In the $V_{ds} > (V_{gs} - V_t) > 0$ case

- I_{ds} Current is effectively constant

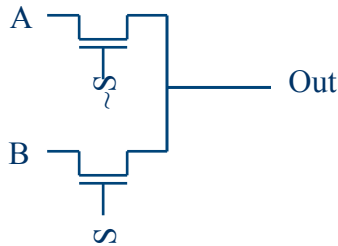
- Channel is “pinched off” and conduction is accomplished by drift of carriers

- Voltage across pinched off channel (i.e. V_{ds}) is fixed at $V_{gs} - V_t$

- This is why you don’t use an N-type to pass 1’s!
- High voltage is degraded by V_t
- Depletion region is lost at $V_{ds} = (V_{gs} - V_t)$

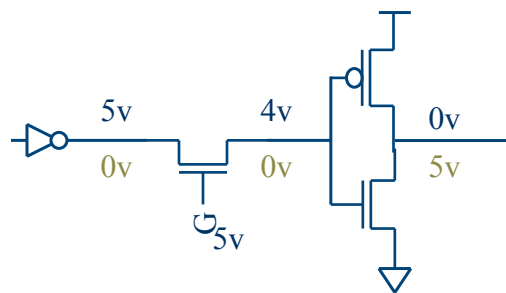


Aside: N-type Pass Transistors



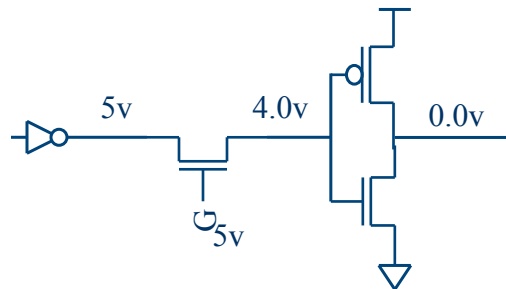
- ◆ If it weren't for the threshold drop, N-type pass transistors (without the P-type transmission gate) would be nice
 - 2-way Mux Example...

N-type Pass Transistors



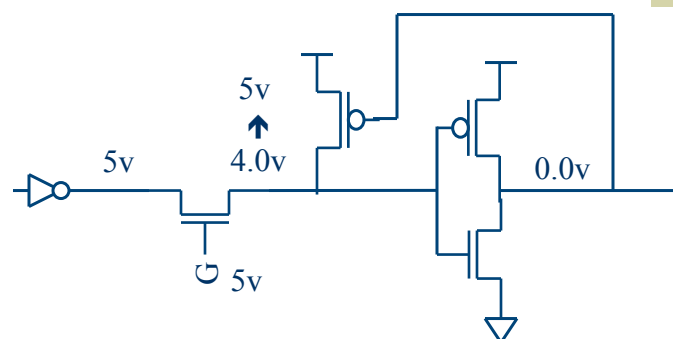
- Is this a good design using an nMOS pass transistor?

N-type Pass Transistors



- On one hand, the degraded high voltage from the pass transistor will be restored by the inverter
- On the other hand, the P-device may not turn off completely resulting in extra power being used

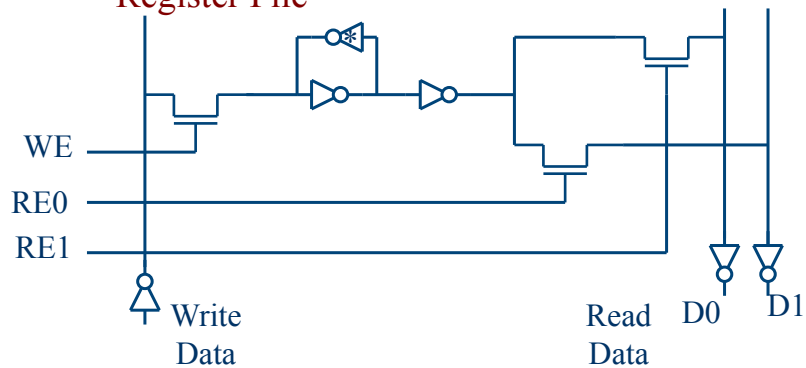
N-type Pass Transistors



- One option is a “keeper” transistor fed back from the output
 - This pulls the internal node high when the output is 0
 - But is disconnected when output is high
- Make sure the size is right...(i.e. weak)

N-type Pass Transistors

- ♦ In practice, they are used fairly often, but be aware of what you're doing
 - For example, read/write circuits in a Register File



Back to the Saturated Transistor

- ♦ What influences the constant I_{ds} in the saturated case?
 - Channel length
 - Channel width
 - Threshold voltage V_t
 - Thickness of gate oxide
 - Dielectric constant of gate oxide
 - Carrier mobility μ
 - Velocity Saturation

Back to the Saturated Transistor

- ♦ What influences the constant I_{ds} in the saturated case?
 - *Channel length*
 - *Channel width*
 - Threshold voltage V_t
 - Thickness of gate oxide
 - Dielectric constant of gate oxide
 - Carrier mobility μ
 - Velocity Saturation

Threshold Voltage: V_t

- ♦ The V_{gs} voltage at which I_{ds} is essentially 0
 - $V_t = .77\text{v}$ for nmos and $-.92\text{v}$ for pmos in our process
 - Tiny I_{ds} is exponentially related to V_{gs} , V_{ds}
 - Take 6770 & 6720 for “subthreshold” circuit ideas
- ♦ V_t is affected by
 - Gate conductor material
 - Gate insulator material
 - Gate insulator thickness
 - Channel doping
 - Impurities at Si/insulator interface
 - Voltage between source and substrate (V_{sb})

Basic DC Equations for I_{ds}

♦ Cutoff Region

- $V_{gs} < V_t$, $I_{ds} = 0$

♦ Linear Region

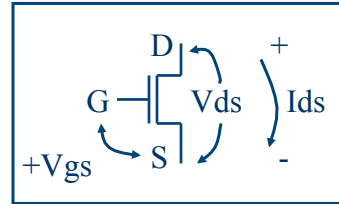
- $0 < V_{ds} < (V_{gs} - V_t)$

$$I_{ds} = \beta[(V_{gs} - V_t)V_{ds} - V_{ds}^2/2]$$

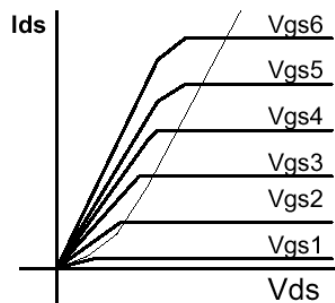
- Note that this is only “linear” if $V_{ds}^2/2$ is very small, i.e. $V_{ds} \ll V_{gs} - V_t$

♦ Saturated Region

- $0 < (V_{gs} - V_t) < V_{ds}$, $I_{ds} = \beta[(V_{gs} - V_t)^2/2]$



I_{ds} Curves



$$\beta = \frac{\mu\epsilon}{t_{ox}} \left(\frac{W}{L} \right) = \mu C_{ox} \left(\frac{W}{L} \right)$$

Cutoff Region

$$V_{gs} < V_t$$

$$I_{ds} = 0$$

Triode (Linear) Region

$$V_{gs} - V_t > V_{ds} > 0$$

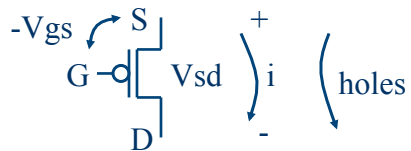
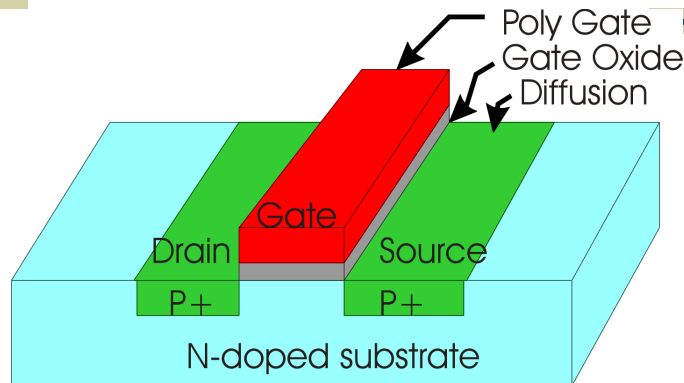
$$I_{ds} = \beta \left[(V_{gs} - V_t)V_{ds} - \frac{V_{ds}^2}{2} \right]$$

Saturation Region

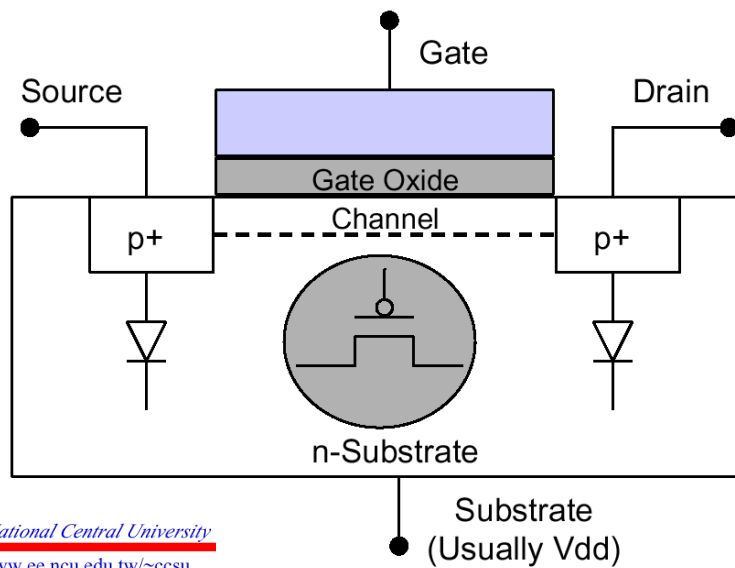
$$V_{ds} > (V_{gs} - V_t) > 0$$

$$I_{ds} = \beta \frac{(V_{gs} - V_t)^2}{2}$$

P-type Transistor

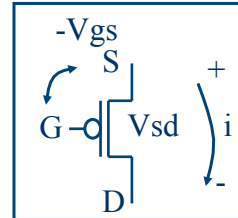


P-type Transistor

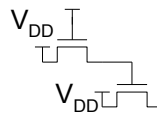
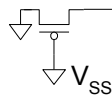
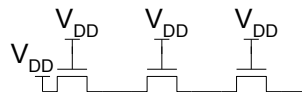
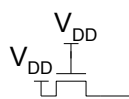


P-type Transistors

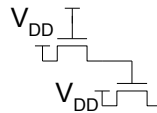
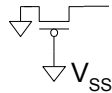
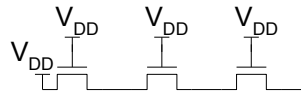
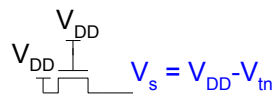
- ◆ Source is Vdd instead of GND
 - $V_{sg} = (V_{dd} - V_{in})$,
 $V_{sd} = (V_{dd} - V_{out})$, V_t is negative
- ◆ **Cutoff:** $(V_{dd} - V_{in}) < -V_t$, $I_{ds} = 0$
- ◆ **Linear Region**
 - $(V_{dd} - V_{out}) < (V_{dd} - V_{in} + V_t)$
 $I_{ds} = \beta[(V_{dd} - V_{in} + V_t)(V_{dd} - V_{out}) - (V_{dd} - V_{out})^2/2]$
- ◆ **Saturated Region**
 - $((V_{dd} - V_{in}) + V_t) < (V_{dd} - V_{out})$
 $I_{ds} = \beta[(V_{dd} - V_{in} + V_t)^2/2]$



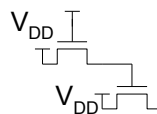
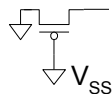
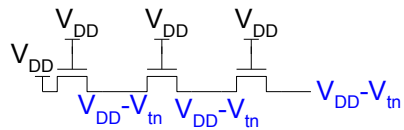
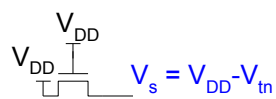
Pass Transistor Ckts



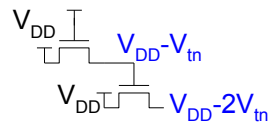
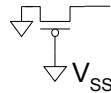
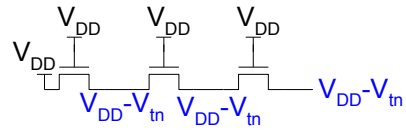
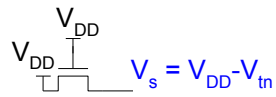
Pass Transistor Ckts



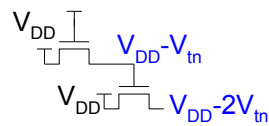
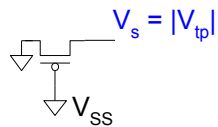
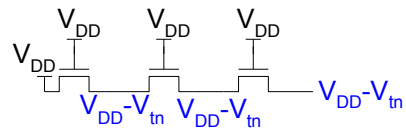
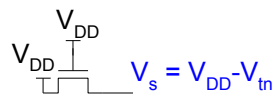
Pass Transistor Ckts



Pass Transistor Ckts



Pass Transistor Ckts



2nd Order Effects

- ♦ Quick introduction to effects that degrade the “digital” assumptions and models we have presented about our transistors so far.
 - This will be covered in more detail in Advanced VLSI 6770
 - You will learn how to relate them to designs
- ♦ Introductory material in this class
 - *In a nutshell – nothing works as well as you think it should! ☹*

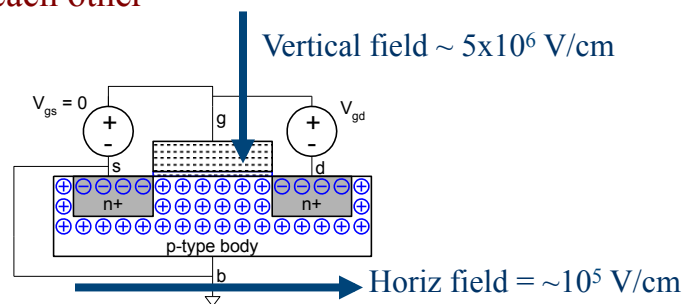
2nd Order Effect: Velocity Saturation

- ♦ With weak fields, current increases linearly with lateral electric field
- ♦ At higher fields, carrier drift velocity rolls off and saturates
 - Due to carrier scattering
 - Result is less current than you think!
 - For a 2μ channel length, effects start around $4v$ Vdd
 - For 180nm, effects start at $0.36v$ Vdd!

*Most important
2nd order effect?*

2nd Order Effect: Velocity Saturation

- ◆ When the carriers reach their speed limit in silicon...
 - Channel lengths have been scaled so that vertical and horizontal EM fields are large and interact with each other



2nd Order Effect: Velocity Saturation

- ◆ When the carriers reach their speed limit in silicon...
 - Means that relationship between I_{ds} and V_{gs} is closer to linear than quadratic
 - Also the saturation point is smaller than predicted
 - For example, 180nm process
 - 1st order model = 1.3v
 - Really is 0.6v

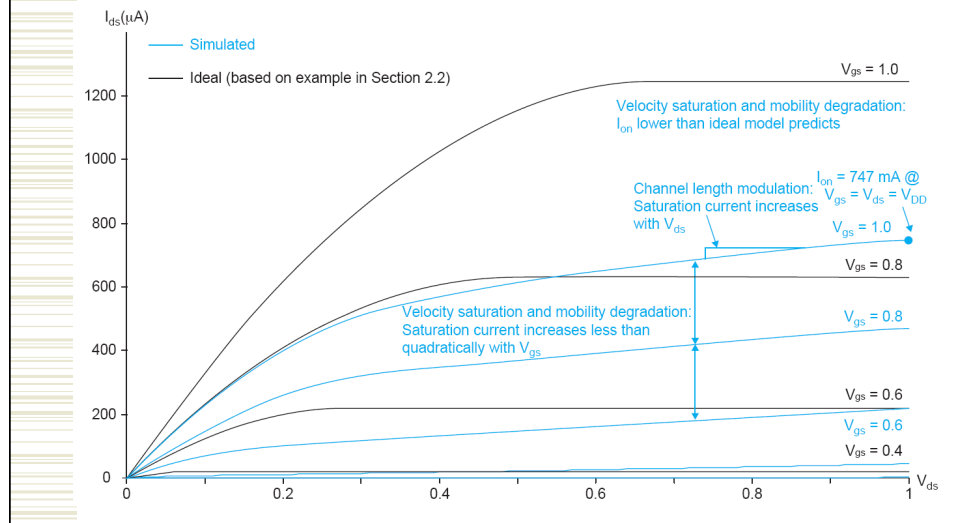
2nd Order Effect: Velocity Saturation

- ◆ This is a basic difference between long- and short-channel devices
 - The strength of the horizontal EM field in a short channel device causes the carriers to reach their velocity limit early
 - Devices saturate faster and deliver less current than the quadratic model predicts

2nd Order Effect: Velocity Saturation

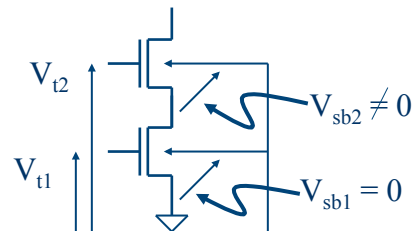
- ◆ Consider two devices with the same W/L ratio in our process ($V_{gs}=5\text{v}$, $V_{dd}=5\text{v}$)
 - 100/20 vs 3/0.6
 - They should have the same current...
 - Because of velocity saturation in the short-channel device, it has ~50% less current!

2nd Order Effect: Velocity Saturation



2nd Order Effect: Body Effect

- ◆ A second order effect that raises V_t
- ◆ Recall that V_t is affected by V_{sb} (voltage between source and substrate)
 - Normally this is constant because of common substrate
 - But, when transistors are in series, V_{sb} ($V_s - V_{\text{substrate}}$) may be different



2nd Order Effect: Body Effect

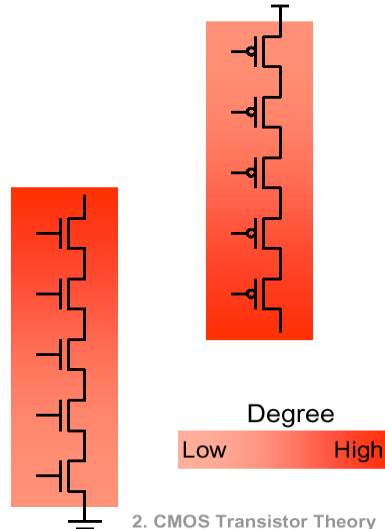
- **Body Effect -**

V_t is a function of voltage between source and substrate

$$V_t = V_{to} + \gamma \sqrt{2\phi_b + |V_{sb}|} + 2\sqrt{\phi_b}$$

$$\phi_b = \frac{kT}{q} \ln\left(\frac{N_A}{N_i}\right)$$

$$\gamma = \frac{t_{ox}}{\epsilon_{ox}} \sqrt{2q\epsilon_{si}N_A} = \frac{1}{C_{ox}} \sqrt{2q\epsilon_{si}N_A}$$



2nd Order Effect: Body Effect

- ♦ Consider an nmos transistor in a 180nm process

- Nominal V_t of 0.4v
- Body is tied to ground
- How much does the V_t increase if the source is at 1.1v instead of 0v?
- Because of the body effect, V_t increases by 0.28v to be 0.68v!

Channel Length Modulation

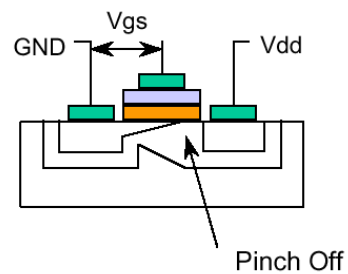
- Channel Length Modulation -**

Channel length is a function of V_{ds} . When V_{ds} increase, the depletion region of the pinch off at drain shorten the channel length.

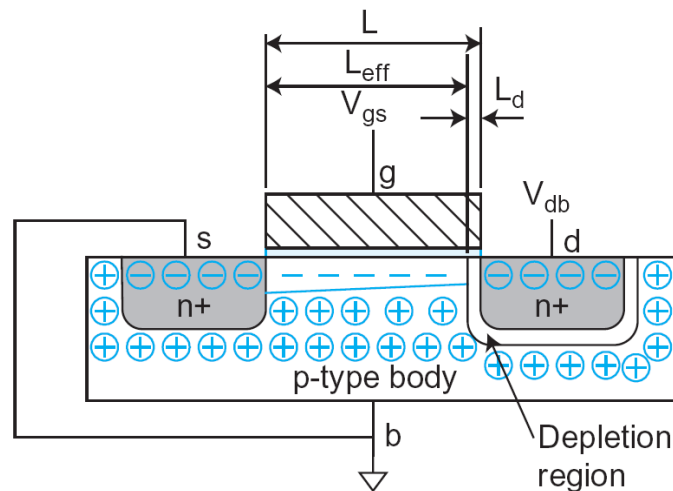
$$L_{eff} = L - L_{short}$$

$$L_{short} = \sqrt{2 \frac{\epsilon_{si}}{qN_A} (V_{ds} - (V_{gs} - V_t))}$$

$$I_{ds} = \frac{kW}{2L} (V_{gs} - V_t)^2 (1 + \lambda V_{ds})$$



Channel Length Modulation



Mobility Variation

- **Mobility Variation -**

The mobility of the carrier decreases when the carrier density increases. Therefore, when V_{gs} is large. The density of the carrier in the channel increases. As a result, the mobility decreases.

$$\mu = \frac{\text{Average_carrier_drift_velocity}(V)}{\text{Electrical_Field}(E)}$$

$$\mu_n = 600 \text{ cm}^2 / V \cdot \text{sec}$$

$$\mu_p = 250 \text{ cm}^2 / V \cdot \text{sec}$$

Other 2nd Order Effects

- **Fowler-Nordheim Tunneling**

When the gate oxide is very thin, a current can flow from gate to source by electron tunneling through the gate oxide.

$$I_{FN} = C_1 W L E_{ox}^2 e^{\frac{-E_o}{E_{ox}}}$$

$$E_{ox} = \frac{V_{gs}}{t_{ox}}$$

- **Drain Punchthrough**

When the drain voltage is high enough, the depletion region around the drain may extend to the source. Thus, causing current to flow irrespective of the gate voltage.

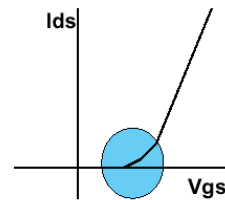
Other 2nd Order Effects

- **Impact Ionization - Hot Electrons**

When the source-drain electric field is too large, the electron speed will be high enough to break the electron-hole pair. Moreover, the electrons will penetrate the gate oxide, causing a gate current.

- **Subthreshold Region**

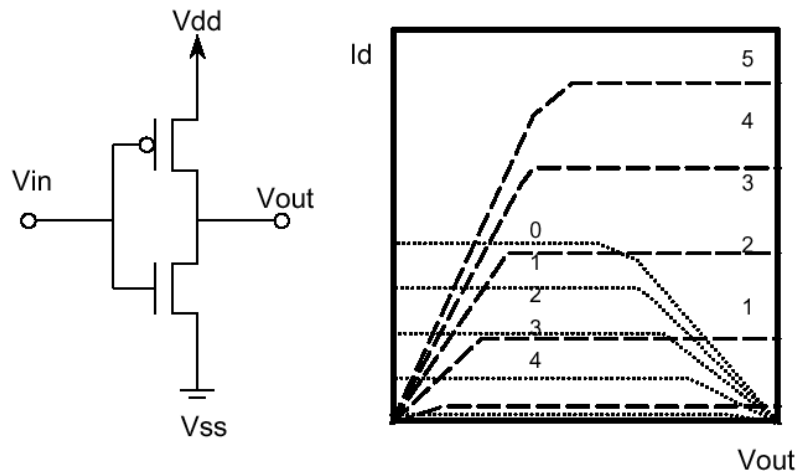
The cutoff region is also referred to as the subthreshold region, where I_{ds} increase exponentially with V_{ds} and V_{gs} .



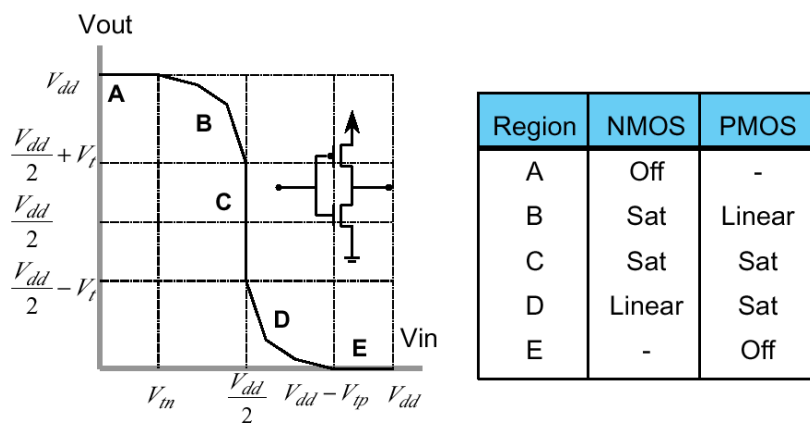
Inverter Switching Point

- ♦ Inverter switching point is determined by ratio of β_n/β_p
 - If $\beta_n/\beta_p = 1$, then switching point is $V_{dd}/2$
- ♦ If W/L of both N and P transistors are equal
 - Then $\beta_n/\beta_p = \mu_n/\mu_p$ = electron mobility / hole mobility
 - This ratio is usually between 2 and 3
 - Means ratio of W_{ptree}/W_{ntree} needs to be between 2 and 3 for $\beta_n/\beta_p = 1$
 - For this class, we'll use $W_{ptree}/W_{ntree} = 2$

Inverter Switching Point



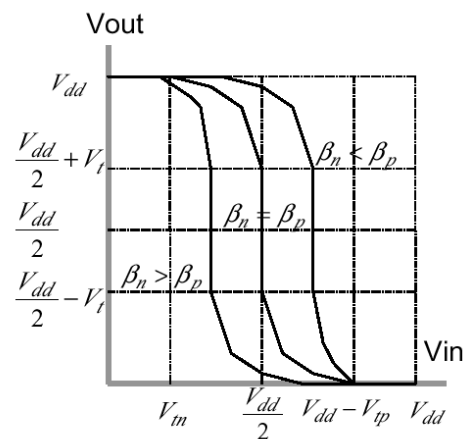
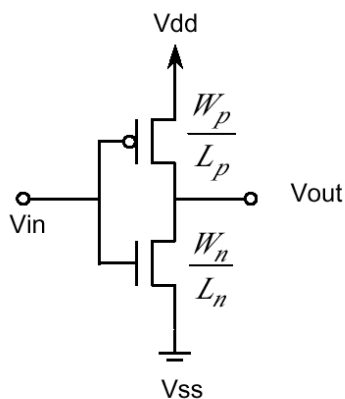
Inverter Operating Regions



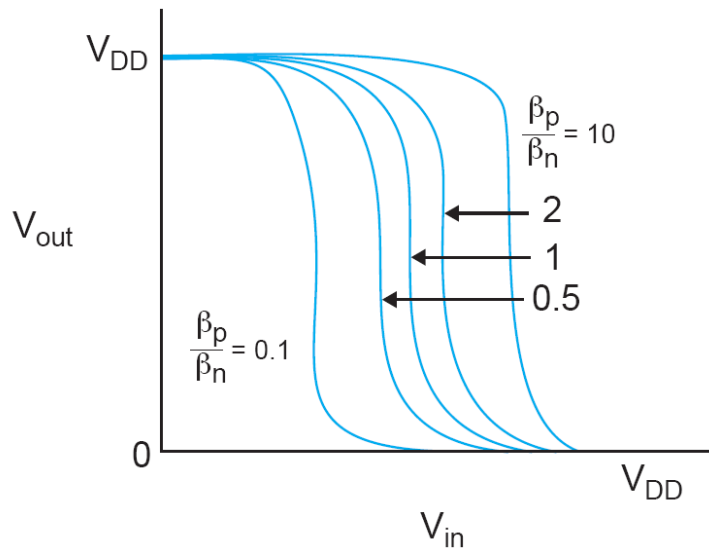
Gate Sizes

- ♦ Assume minimum inverter is $W_p/W_n = 2/1$ ($L = L_{min}$, $W_n = W_{min}$, $W_p = 2W_n$)
 - This becomes a 1x inverter
- ♦ To drive larger capacitive loads, you need more gain, more I_{ds}
 - Double W_n and W_p to get 2x inverter
 - W_p/W_n is still 2/1, but inverter has twice the gain (current drive)
 - Not always a linear relationship...

Inverter β Ratios

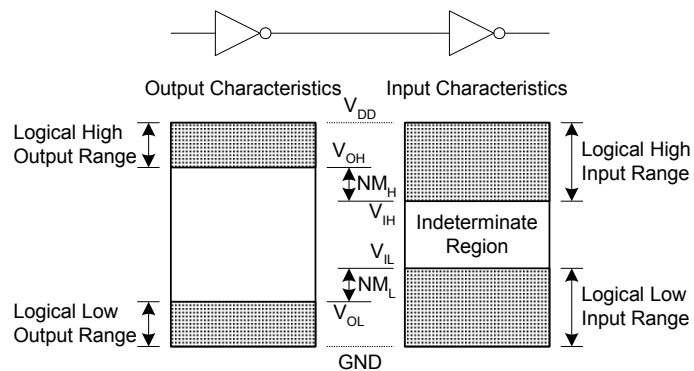


Inverter β Ratios



Inverter Noise Margin

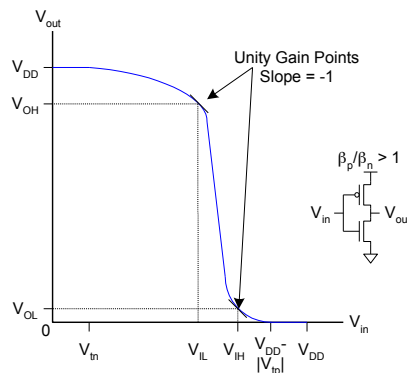
How much noise can a gate see before it doesn't work right?



Inverter Noise Margin

- ▶ To maximize noise margins, select logic levels at:

- ▶ Unity gain point of DC transfer characteristic



Performance Estimation

- ♦ First we need to have a model for resistance and capacitance
 - Delays are caused (to first order) by RC delays charging and discharging capacitors
- ♦ All these layers on the chip have R and C associated with them
- ♦ Low level analog circuit simulations
 - Spectre or HSPICE
- ♦ High level PrimeTime simulations
 - In 6770...

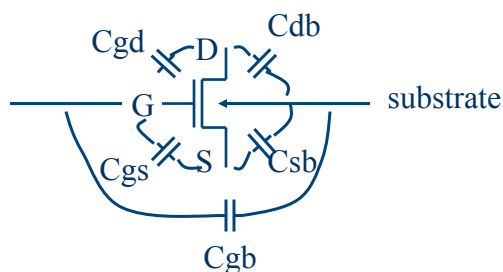
Resistance

- ♦ $R = (\rho/t)(L/W) = R_s(L/W)$
 - ρ = resistivity of the material
 - t = thickness
 - R_s = sheet resistance in Ω/square
- ♦ Typical values of R_s in our process

	Min	Typ	Max
M3	0.04	0.05	0.08
M1, M2	0.07	0.08	0.1
Poly	20	25	40
Poly2	40	50	60
N(P)-active	60 (70)	90 (120)	120 (160)
Nwell	1k	2k	5k

Capacitance

- ♦ Three main forms:
 - Gate capacitance (gate of transistor)
 - Diffusion capacitance (drain regions)
 - Routing capacitance (metal, etc.)




$$C_g = C_{gb} + C_{gs} + C_{gd}$$

Approximated by
 $C = C_{ox}A$
 C_{ox} = thin oxide cap
 A = area of gate

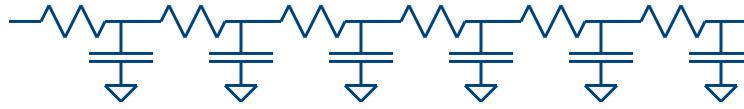
Routing Capacitance

- ♦ First order effect is layer->substrate
 - Approximate using parallel plate model
 - $C = (\epsilon/t)A$
 - ϵ = permittivity of insulator
 - t = thickness of insulator
 - A = area
 - Fringing fields increase effective area
- ♦ Capacitance between layers becomes very complex to simulate!
 - Crosstalk issues...

Distributed RC on Wires

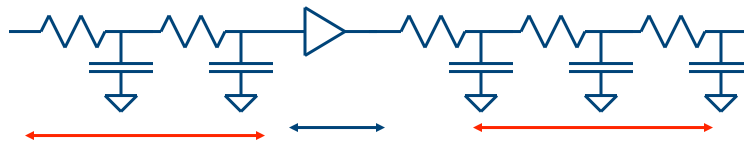
- ♦ Wires look like distributed RC delays
 - Long resistive wires can look like transmission lines
 - Inserting buffers can really help delay
- 
- ♦ $T_n = RC_n(n+1)/2$
 - ♦ $T = KRCL^2/2$ as the number of segments becomes large
 - K = constant (i.e. 0.7) (accounts for rise/fall times)
 - R = resistance per unit length
 - C = capacitance per unit length
 - L = length of wire

RC Wire Delay Example



- ♦ $R = 20\Omega/\text{sq}$
- ♦ $C = 4 \times 10^{-4} \text{ pF}/\mu\text{m}$
- ♦ $L = 2\text{mm}$
- ♦ $K = 0.7$
- ♦ $T = KRCL^2/2$
- ♦ $T = (0.7) (20) (4 \times 10^{-15})(2000)^2 / 2 \text{ s}$
 - delay = 11.2 ns

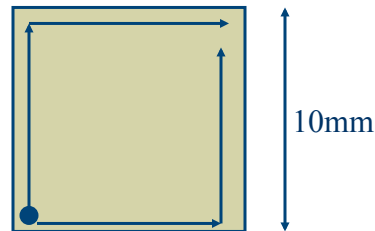
RC Wire/Buffer Delay Example



- ♦ Now split into 2 segments of 1mm with a buffer
- ♦ $T = 2 \times (0.7)(20)(4 \times 10^{-15})(1000)^2/2 + T_{\text{buf}}$
 $= 5.6\text{ns} + T_{\text{buf}}$
- ♦ Assuming T_{buf} is less than 5.6ns
 (which it will be), the split wire is a win

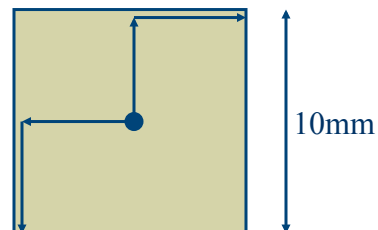
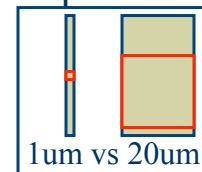
Another Example: Clock

- ♦ 50pF clock load distributed across 10mm chip in 1μm metal
 - Clock length = 20mm
 - $R = 0.05\Omega/\text{sq}$, $C = 50\text{pF}/20\text{mm}$
 - $T = (0.7)(RC/2)L^2 = (0.7)(6.25 \times 10^{-17})(20,000)^2 = 17.5\text{ns}$



Different Distribution Scheme

- ♦ Put clock driver in the middle of the chip
- ♦ Widen clock line to 20μm wires
 - Clock length = 10mm
 - $R = 0.05\Omega/\text{sq}$, $C = 50\text{pF}/20\text{mm}$
 - $T = (0.7)(RC/2)L^2 = (0.7)(0.31 \times 10^{-17})(10,000)^2 = 0.22\text{ns}$
 - Reduces R by a factor of 20, L by 2 ☺
 - Increases C a little bit (clock load still 50pF)



Capacitance Design Guide

- ◆ Get a table of typical capacitances per unit square for each layer
 - Capacitance to ground
 - Capacitance to another layer
- ◆ Add them up...
- ◆ See, for example, Figure 6.12 in your text

Capacitance Design Guide

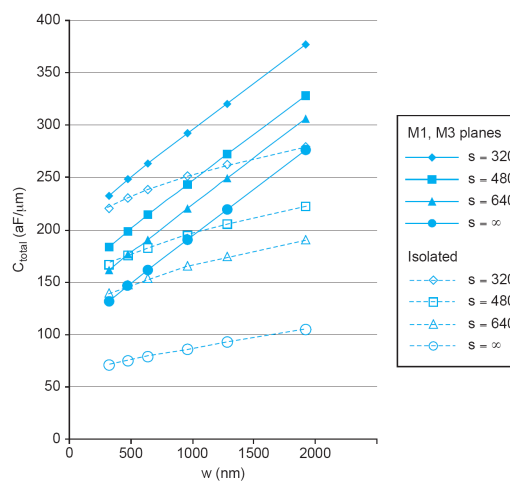


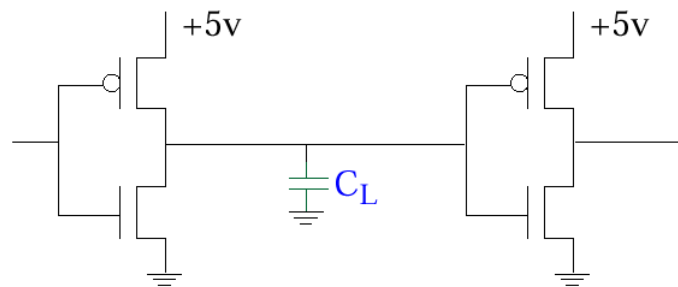
FIGURE 6.12 Capacitance of metal2 line as a function of width and spacing

Wire Length Design Guide

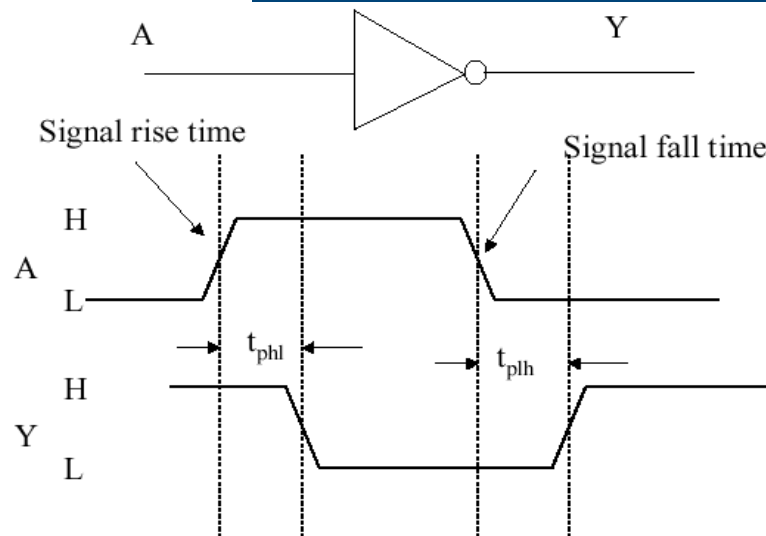
- ◆ How much wire can you use in a conducting layer before the RC delay approaches that of a unit inverter?
 - Metal3 = 2,500u
 - Metal2 = 2,000u
 - Metal1 = 1,250u
 - Poly = 50u
 - Active = 15u

Propagation Delay

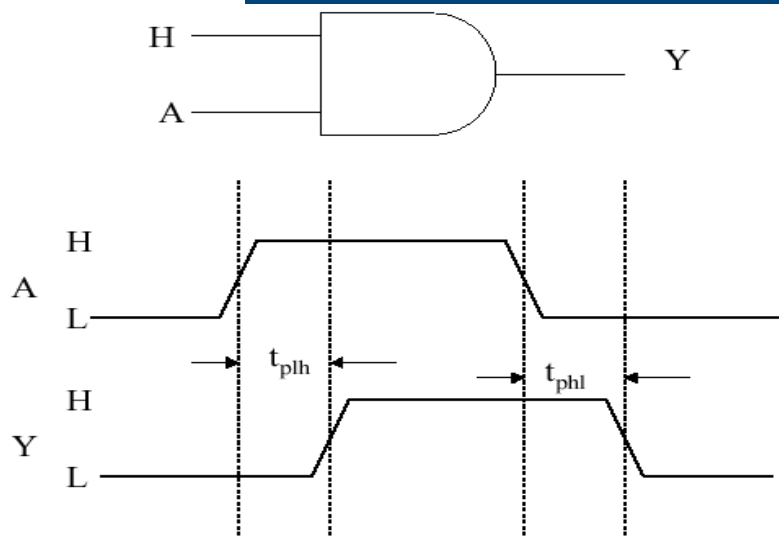
- Recall that it takes time to charge capacitors
- Recall that the gate of a transistor looks like a capacitor
- Wires have resistance and capacitance also!



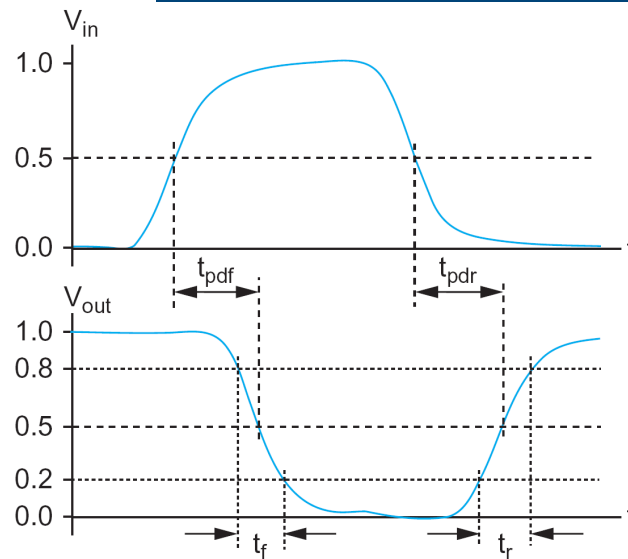
Inverter Propagation Delay



Non-Inverting Delay



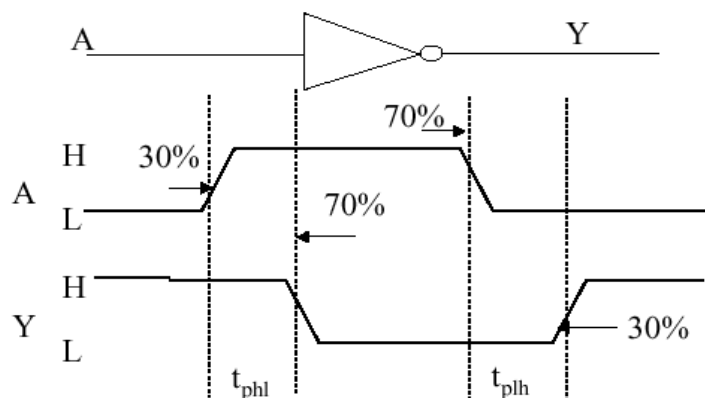
Propagation Delay



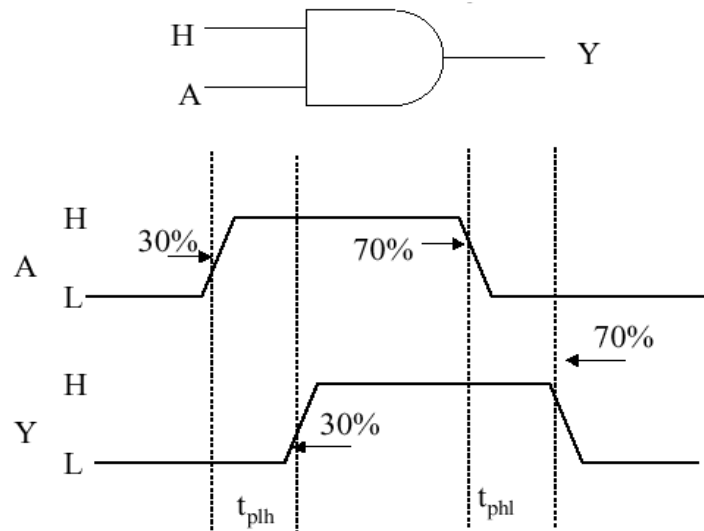
Where to Measure Delay?

If use 50% point (input) to 50% point (output), can produce negative delays (slow input slope, fast output slope).

A better way is to use the 30% and 70% points on the signals.



Example Non-Inverting Gate

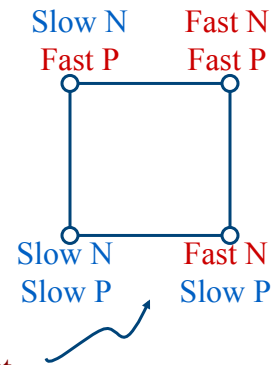


What Affects Gate Delay?

- ◆ Environment
 - Increasing V_{dd} improves delay
 - Decreasing temperature improves delay
 - Fabrication effects, fast/slow devices
- ◆ Usually measure delay for at least three cases:
 - Best - high V_{dd} , low temp, fast N, Fast P
 - Worst - low V_{dd} , high temp, slow N, Slow P
 - Typical - typ V_{dd} , room temp (25C), typ N, typ P

Process Corners

- ◆ When parts are specified, under what operating conditions?
- ◆ **Temp:** three ranges
 - Commercial: 0 C to 70 C
 - Industrial: -40 C to 85 C
 - Military: -55 C to 125 C
- ◆ **Vdd:** Should vary $\pm 10\%$
 - 4.5 to 5.5v for example
- ◆ **Process variation:**
 - Each transistor type can be slow or fast



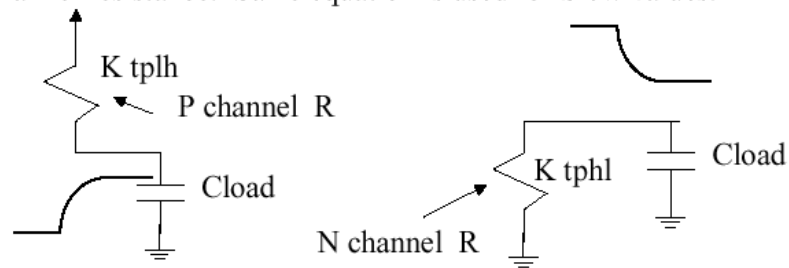
What Else Affects Gate Delay?

Input slew and output load both effect timing. For a FIXED input slope, FIXED environment, a simple timing model is:

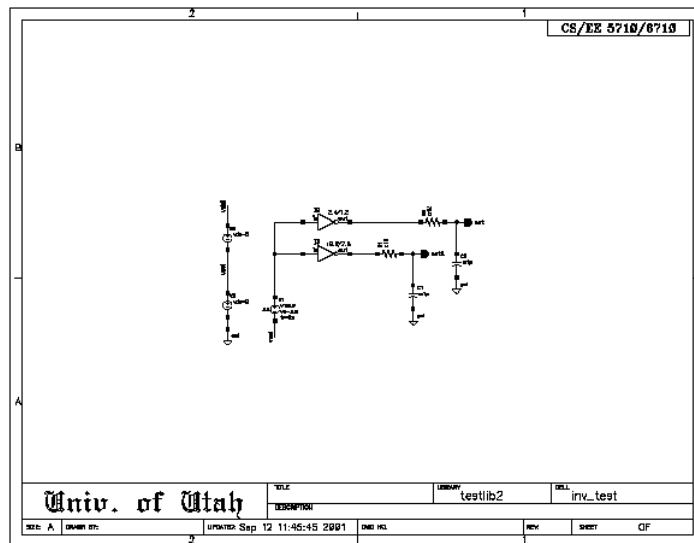
$$\text{delay} = T_{\text{noload}} + K * C_{\text{load}}$$

T_{noload} is the delay of the gate with no external load.

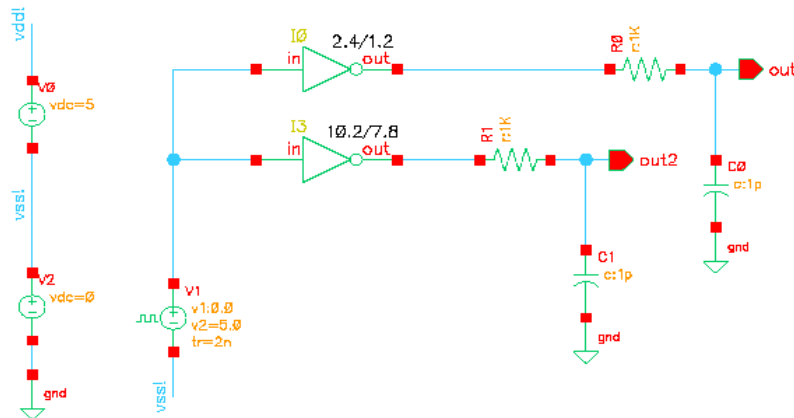
K is different for TPLH, TPHL since it represents the channel resistance. Same equation is used for Slew values.



Inv_Test Schematic



Closeup of Inv-Test

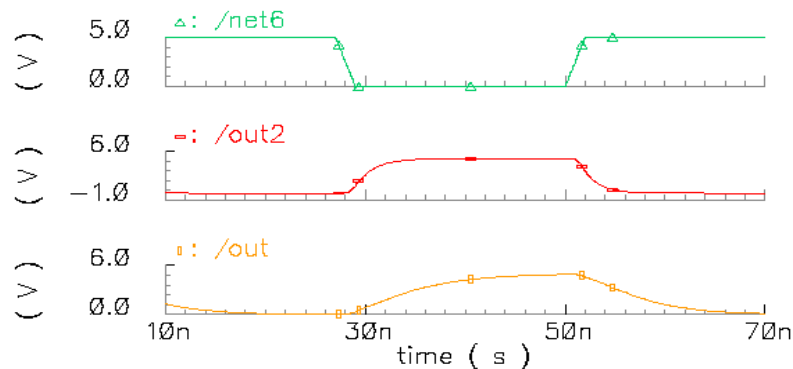


◆ Note the sizes I used for this example...

Analog Simulation Output

testlib2 inv_test config : Sep 12 11:21:44 2001

Transient Response



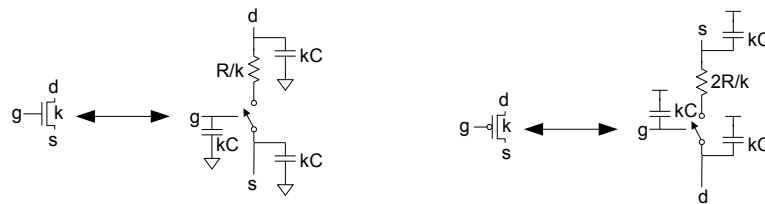
- ◆ Note different waveforms for different sizes of transistors

Effective Resistance

- ◆ Shockley models have limited value
 - Not accurate enough for modern transistors
 - Too complicated for much hand analysis
- ◆ Simplification: treat transistor as resistor
 - Replace $I_{ds}(V_{ds}, V_{gs})$ with effective resistance R
 - $I_{ds} = V_{ds}/R$
 - R averaged across switching of digital gate
- ◆ Too inaccurate to predict current at any given time
 - But good enough to predict RC delay

RC Delay Model

- ♦ Use equivalent circuits for MOS transistors
 - Ideal switch + capacitance and ON resistance
 - Unit nMOS has resistance R , capacitance C
 - Unit pMOS has resistance $2R$, capacitance C
- ♦ Capacitance proportional to width
- ♦ Resistance inversely proportional to width

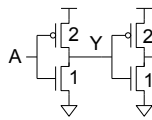


RC Values

- ♦ Capacitance
 - $C = C_g = C_s = C_d = 2 \text{ fF}/\mu\text{m}$ of gate width
 - Values similar across many processes
- ♦ Resistance
 - $R \approx 6 \text{ K}\Omega \cdot \mu\text{m}$ in $0.6\mu\text{m}$ process
 - Improves with shorter channel lengths
- ♦ Unit transistors
 - May refer to minimum contacted device ($1.2\mu/0.6\mu$)
 - Or maybe $1 \mu\text{m}$ wide device
 - Doesn't matter as long as you are consistent

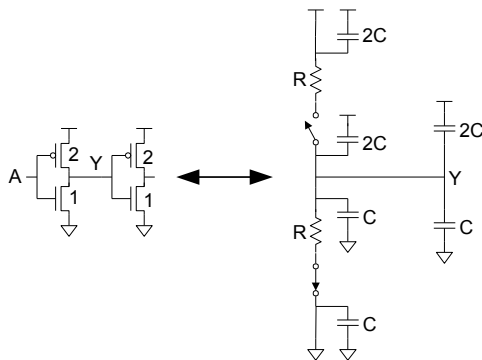
Inverter Delay Estimate

- ◆ Estimate the delay of a fanout-of-1 inverter



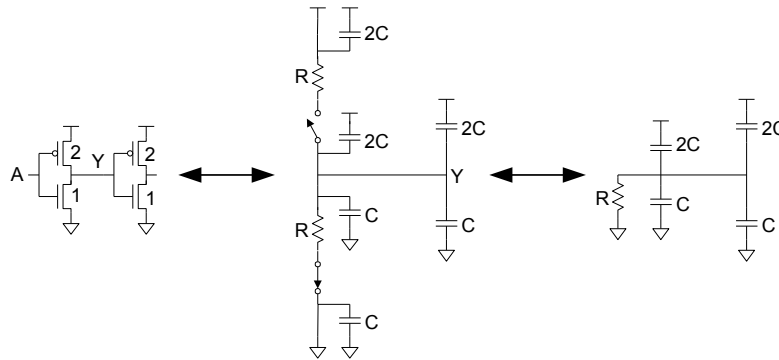
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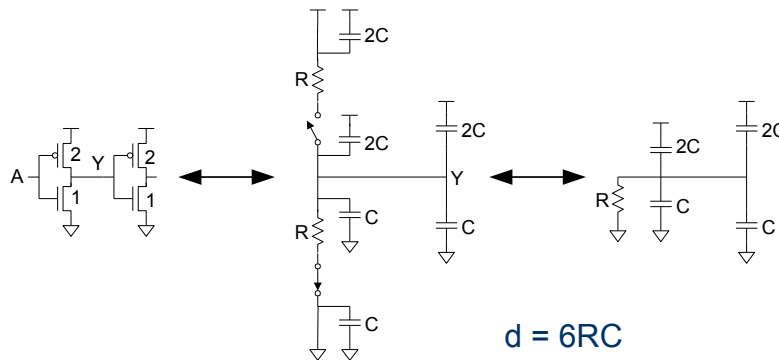
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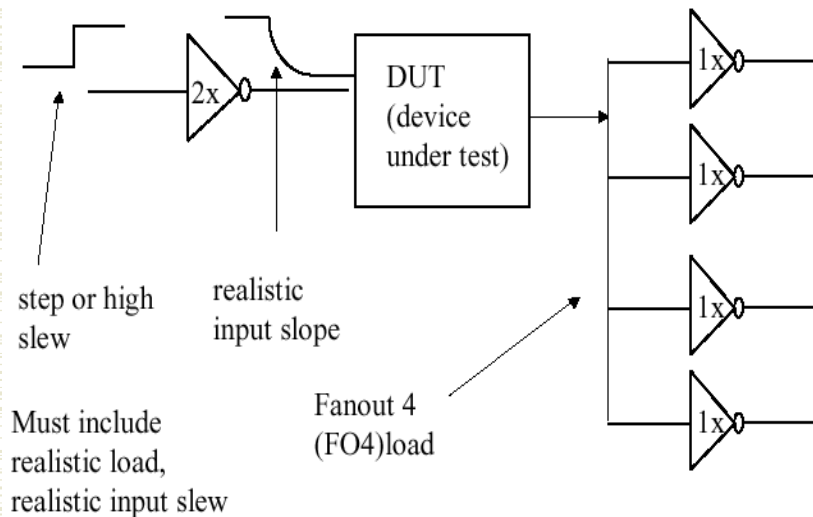


Inverter Delay Estimate

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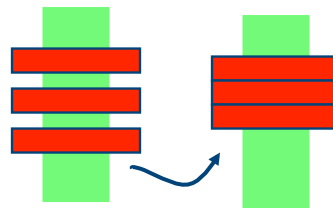


What's a Standard Load?



What About Gates in Series

- ◆ Basically we want every gate to have the delay of a “standard inverter”
 - Standard inverter starts with 2/1 P/N ratio
- ◆ Gates in series? Sum the conductance to get the series conductance
- ◆ $\beta_{n\text{-eff}} = 1 / (1/\beta_1 + 1/\beta_2 + 1/\beta_3)$
 - $\beta_{n\text{-eff}} = \beta_n / 3$
- ◆ Effect is like increasing L by 3
 - Compensate by increasing W by 3



Power Dissipation

- ♦ Three main contributors:
 1. Static leakage current (P_s)
 2. Dynamic short-circuit current during switching (P_{sc})
 3. Dynamic switching current from charging and discharging capacitors (P_d)
- ♦ Becoming a HUGE problem as chips get bigger, clocks get faster, transistors get leakier!
 - Power typically gets dissipated as heat...

Static Leakage Power

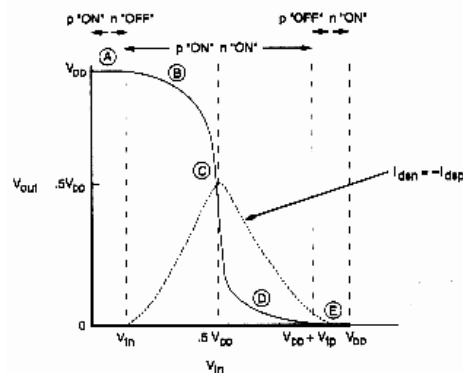
- ♦ Small static leakage current due to:
 - Reverse bias diode leakage between diffusion and substrate (PN junctions)
 - Subthreshold conduction in the transistors
- ♦ Leakage current can be described by the diode current equation
 - $I_o = i_s(e^{qV/kT} - 1)$
 - Estimate at 0.1nA – 0.5nA per device at room temperature

Static Leakage Power

- ♦ That's the leakage current
- ♦ For static power dissipation:
 - $P_s = \text{SUM of } (I \times V_{dd})$ for all n devices
 - For example, inverter at 5v leaks about 1-2 nW in a .5u technology
 - Not much...
 - ...but, it gets MUCH worse as feature size shrinks!

Short-Circuit Dissipation

- ♦ When a static gate switches, both N and P devices are on for a short amount of time
 - Thus, current flows during that switching time



Short-Circuit Dissipation

- ♦ So, with short-circuit current on every transition of the output, integrate under that current curve to get the total current
 - It works out to be:
 - $P_{sc} = \beta/12(V_{dd} - 2V_t)^3 (T_{rf} / T_p)$
 - Assume that $T_r = T_f$, $V_{tn} = -V_{tp}$, and $\beta_n = \beta_p$
 - Note that P_{sc} depends on B , and on input waveform rise and fall times

Short-Circuit Dissipation

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 - Assume that $T_r = T_f$, $V_{tn} = -V_{tp}$, and $\beta_n = \beta_p$
 - Note that P_{sc} depends on B , and on input waveform rise and fall times
- In practice – unless input edge rate is a LOT slower than the output edge rate this is a small fraction of the total current, and is usually negligible...*

Dynamic Dissipation

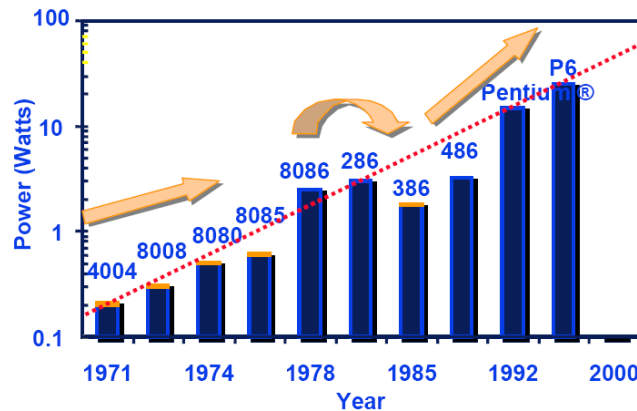
- ♦ Charging and discharging all those capacitors!
 - By far the largest component of power dissipation
 - $P_d = C_L V_{dd}^2 f$
- ♦ Watch out for large capacitive nodes that switch at high frequency
 - Like clocks...

Total Power

- ♦ These are pretty rough estimates
- ♦ It's hard to be more precise without CAD tool support
 - It all depends on frequency, average switching activity, number of devices, etc.
 - There are programs out there that can help
- ♦ But, even a rough estimate can be a valuable design guide
- ♦ $P_{total} = P_s + P_{sc} + P_d$

Power Dissipation

- Lead microprocessor power continues to increase



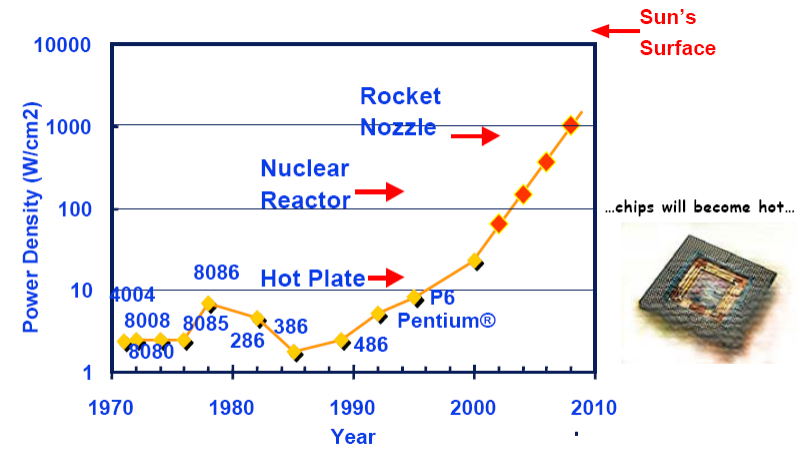
- Power delivery and dissipation will be prohibitive

Source: Borkar, De Intel®

Heat Dissipation

- ♦ 60 W light bulb has surface area of 120 cm²
- ♦ Core2 Duo die dissipates 75 W over 1.4 cm²
 - Chips have enormous power densities
 - Cooling is a serious challenge
- ♦ Graphics chips even worse
 - NVIDIA GTX480 – 250 W in ~3 cm²
- ♦ Package spreads heat to larger surface area
 - Heat sinks may increase surface area further
 - Fans increase airflow rate over surface area
 - Liquid cooling used in extreme cases (\$\$\$)

Chip Power Density

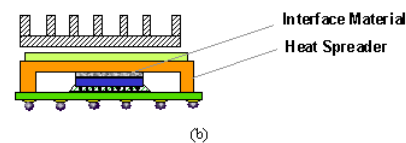
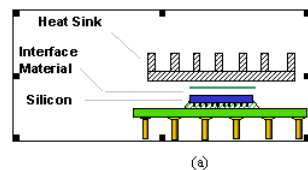


$$P=VI: 75W @ 1.5V = 50 A!$$

Source: Borkar, De Intel©

Thermal Solutions

- ♦ Heat sink
 - Mounted on processor package
- ♦ Passive cooling
 - Remote system fan
- ♦ Active cooling
 - Fan mounted on sink
- ♦ Heat spreaders
 - Increase surface area
 - Example: Metal plate under laptop keyboard



a. Heat sink mounting for low-power chip
b. Package design for high-power chips

"Thermal Challenges during Microprocessor Testing", Intel Technology Journal, Q3 2000

Alternative View of “Computing Power”

Environmental burden of CPUs!

- Total power consumption of CPUs in world's PCs:

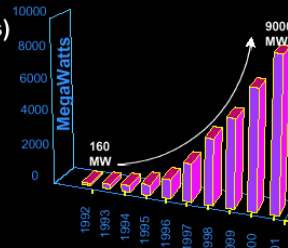
1992: 160 MWatts (87M CPUs)

2001: **9,000 MWatts** (500M CPUs)

- That's 4 Hoover Dams!



Courtesy: United States Department of the Interior
Bureau of Reclamation - Lower Colorado Region



[Source: Dataquest (for installed base) +
estimates for avg. installed CPU power]
Projected with Pentium™ Power



Andy's vision: 1 Billion Connected PCs!

Courtesy Avi Mendelson, Intel.

Power Management on Pentium 4

- ◆ Over 400 power-saving features!
 - 20% of features = 75% of saved power
- ◆ Clock throttling
 - Thermal diode temperature sensor
 - Stop clock for a few microseconds
 - Output pin can be used by system to trigger other responses
- ◆ SpeedStep technology for mobile processors
 - Switch to lower frequency and voltage
 - Depends on whether power source is battery or AC
 - Can be manually overridden by Windows control panel

“Managing the Impact of Increasing Microprocessor Power Consumption”, Intel Technology Journal, Q1 2001

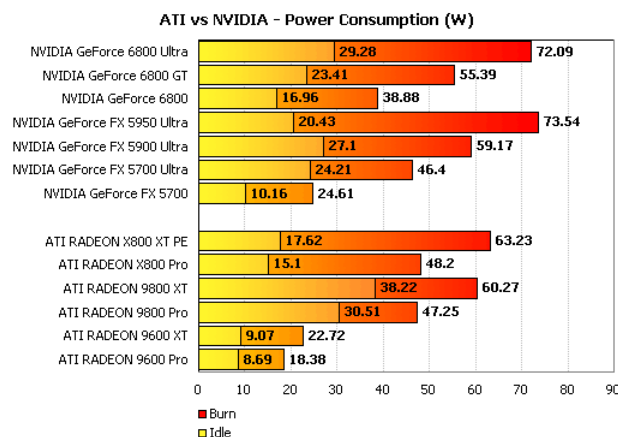
Pentium 4 Multi-level Powerdown

- ♦ Level 0 = Normal operation (includes thermal throttle)
- ♦ Level 1 = Halt instructions (less processor activity)
- ♦ Level 2 = Stop Clock (internal clocks turn off)
- ♦ Level 3 = Deep sleep (remove chip input clock)
- ♦ Level 4 = Deeper sleep (lower Vdd by 66%)
 - For “extended periods of processor inactivity”
 - QuickStart technology – resume normal operation from Deeper Sleep
- ♦ Note: We haven’t even talked about system powerdown modes, like removing power from processor, stopping hard disks, dimming or turning off the display...

“Managing the Impact of Increasing Microprocessor Power Consumption”, Intel Technology Journal, Q1 2001

Graphics Card Power

<http://www.xbitlabs.com/articles/video/display/ati-vs-nv-power.html>

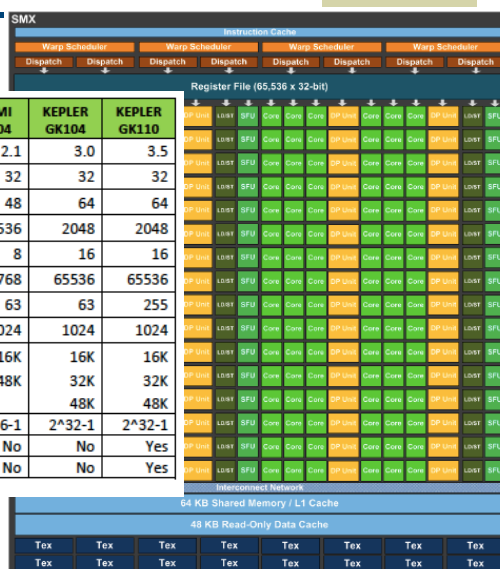


$P=VI: 75W @ 1.5V = 50 A!$

Graphics Card Power

- 3GHz P4 (2005): 6 GFLOPS peak ~65-115watts
- NVIDIA GeForce FX5900 (2004): 53 GFLOPS
 - 128 FP units in parallel at 450MHz
- NVIDIA GeForce 7800 (2006) GTX512: 200 GFLOPS
 - 192 FP units at 550 MHz, 80 watts
- NVIDIA GeForce GTX 480 (2010): 1.35 TFLOPS
 - 480 cores, 1.4GHz, 250 watts... 105°C
 - 1.5 GB GDDR5, 384 bit interface, 177.4 GB/sec
 - 3B transistors in 40nm CMOS

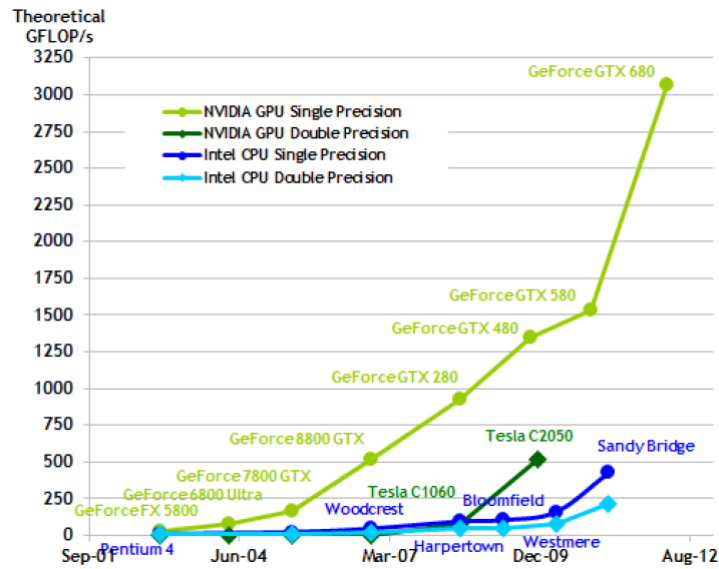
Graphics Chip Architecture

	FERMI GF100	FERMI GF104	KEPLER GK104	KEPLER GK110																
Compute Capability	2.0	2.1	3.0	3.5																
Threads / Warp	32	32	32	32																
Max Warps / Multiprocessor	48	48	64	64																
Max Threads / Multiprocessor	1536	1536	2048	2048																
Max Thread Blocks / Multiprocessor	8	8	16	16																
32-bit Registers / Multiprocessor	32768	32768	65536	65536																
Max Registers / Thread	63	63	63	255																
Max Threads / Thread Block	1024	1024	1024	1024																
Shared Memory Size Configurations (bytes)	16K 48K	16K 48K	16K 32K 48K	16K 32K 48K																
Max X Grid Dimension	2^16-1	2^16-1	2^32-1	2^32-1																
Hyper-Q	No	No	No	Yes																
Dynamic Parallelism	No	No	No	Yes																

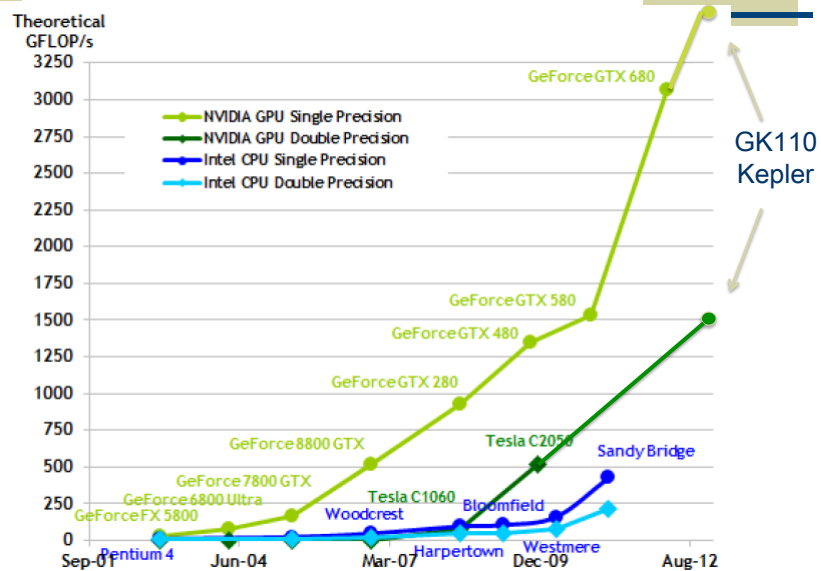
Compute Capability of Fermi and Kepler GPUs

64 KB Shared Memory / L1 Cache							
48 KB Read-Only Data Cache							
Tex	Tex	Tex	Tex	Tex	Tex	Tex	Tex
Tex	Tex	Tex	Tex	Tex	Tex	Tex	Tex

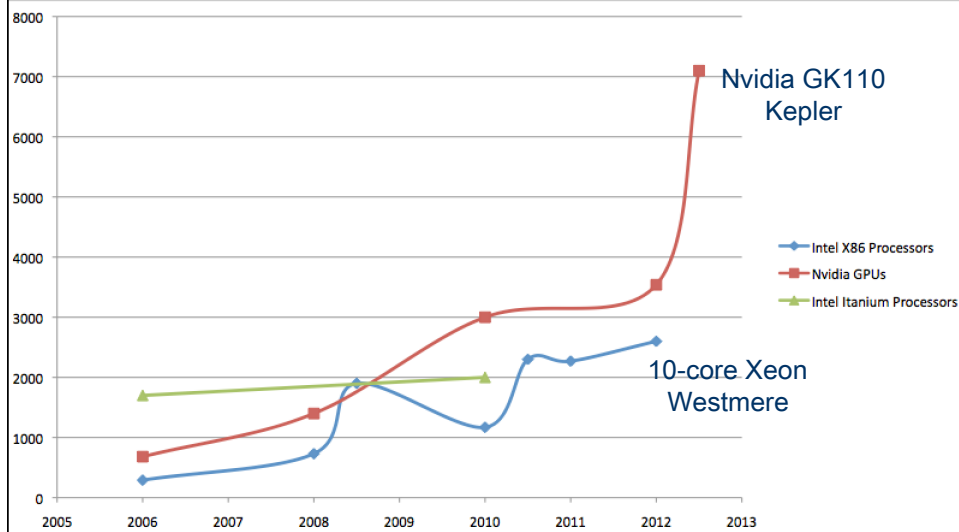
Graphics Chips Performance



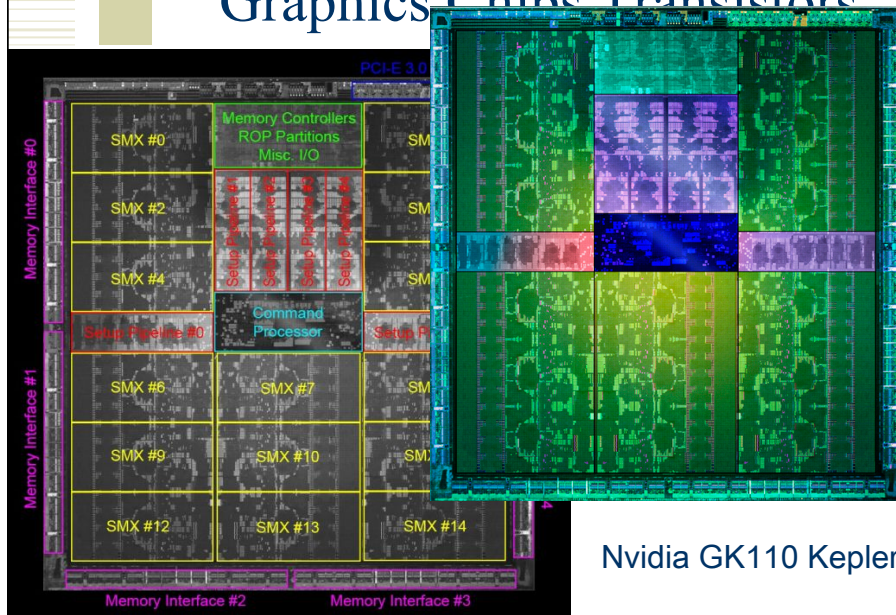
Graphics Chips Performance



Graphics Chips Transistors



Graphics Chips Transistors



Nvidia GK110 Kepler

Graphics Cards

